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Optimal eye movement strategies in visual search

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To perform visual search, humans, like many mammals, encode a large field of view with retinas having variable spatial resolution, and then use high-speed eye movements to direct the highest-resolution region, the fovea, towards potential target locations^{1,2}. Good search performance is essential for survival, and hence mammals may have evolved efficient strategies for selecting fixation locations. Here we address two questions: what are the optimal eye movement strategies for a foveated visual system faced with the problem of finding a target in a cluttered environment, and do humans employ optimal eye movement strategies during a search? We derive the ideal bayesian observer^{3–6} for search tasks in which a target is embedded at an unknown location within a random background that has the spectral characteristics of natural scenes⁷. Our ideal searcher uses precise knowledge about the statistics of the scenes in which the target is embedded, and about its own visual system, to make eye movements that gain the most information about target location. We find that humans achieve nearly optimal search performance, even though humans integrate information poorly across fixations^{8–10}. Analysis of the ideal searcher reveals that there is little benefit from perfect integration across fixations—much more important is efficient processing of information on each fixation. Apparently, evolution has exploited this fact to achieve efficient eye movement strategies with minimal neural resources devoted to memory.

Recent decades have seen considerable progress in understanding visual search^{11,12}, eye movements^{1,2,13} and active robotic vision¹⁴; however, there is no formal theory of optimal eye movement strategies in conducting visual search. Such a theory would provide insight into the design requirements for effective control of eye movements and attention, and hence could serve as a powerful framework for analysing the behaviour and neurophysiology of eye movements and attention, and for developing robotic applications.

We consider the task of finding a known target that is embedded (added) at a random location in backgrounds of spatial $1/f$ noise, which have the same spatial power spectra as images of natural scenes⁷. Figure 1a shows the target (a spatial sine wave) and a sample of $1/f$ noise.

Not surprisingly, the optimal eye movement strategy depends critically on how the visibility (detectability) of the target varies across the retina. Thus, to specify the ideal searcher, it is necessary first to characterize the visibility maps of the visual system under consideration, for the targets and backgrounds of interest.

To characterize the visibility map for each of the conditions in the search experiment described below, detection accuracy was measured for the sine-wave target as a function of target contrast and background noise contrast, at the 25 spatial locations indicated by the small circles in Fig. 1a. The observer fixated on the centre of the display, which was monitored with an eye tracker, and for each block of trials the target was presented at only a single known location. Figure 1b shows the measurements of detection accuracy (psychometric functions) in the fovea, as a function of target contrast. Each curve is for a different root-mean-squared (r.m.s.) contrast of the noise background, where the r.m.s. contrast is defined as the standard deviation of the pixel luminance divided by the mean luminance. Each of these psychometric functions can

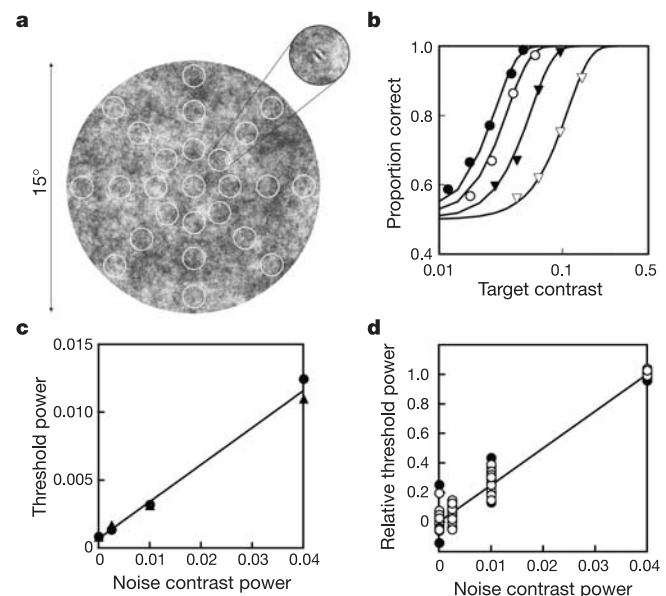


Figure 1 Measurement of the visibility maps. **a**, The target was a windowed sine-wave grating (see inset). Target visibility was measured at each of the locations indicated by the circles (which were not in the stimulus), in a two-interval forced-choice detection task. Each interval was 250 ms, the approximate duration of single fixations in our visual search experiments (280 ms). **b**, Proportion of correct responses in the fovea, as a function of target contrast, for four levels of background noise contrast: filled circles, 0; open circles, 0.05; filled triangles, 0.10; open triangles, 0.20. **c**, Detection threshold power in the fovea for two observers, J.N. (circles) and W.G. (triangles). **d**, Relative threshold power for all measured locations in **a**. These plots were obtained by normalizing the data so that the best-fitting line in each condition had an intercept of 0 and a value of 1.0 at a contrast power of 0.04. Observers: filled circles, J.N.; open circles, W.G.

be summarized by a contrast threshold value, the target contrast that is detected with 82% accuracy, and by a parameter that describes the steepness of the function (see Methods). Figure 1c plots the foveal contrast thresholds (in units of contrast power—the square of the contrast) for two observers. The thresholds fall approximately along a straight line, in agreement with previous studies using white-noise backgrounds^{15–17}. Figure 1d plots the relative threshold (see the figure legend) as a function of noise contrast power for all the retinal locations. The relative thresholds cluster around a straight line, showing that an approximately linear relationship holds for all retinal locations tested; however, there are systematic changes in the slopes and intercepts of the lines with the distance of the target from the fovea (the retinal eccentricity), as shown in Fig. 2a, b. These slope and intercept functions (together with the steepness parameter of the psychometric function) can be used to determine the visibility map for any combination of target and background contrast. Figure 2c shows a cross-section of the maps for two of the conditions in the search experiment described later. Each map specifies, for every retinal eccentricity, the value of a signal-to-noise ratio, d' , which is monotonically related to detection accuracy (see Methods)³.

Now consider the ideal searcher for the relatively simple search task in which the target location is unknown but the stimulus is presented briefly so that no eye movements are possible. In this case, the optimal method is template matching (that is, cross-correlation)^{3,4}. At each potential target location, the retinal image is multiplied by a template of the target and the product is integrated to obtain a template response. If all target locations have equal prior probability, and if the visibility map is flat, then the location with the largest template response is the most likely location of the target (that is, the location with the greatest posterior probability). To compute posterior probabilities when the visibility map is not flat,

template responses are weighted by the visibility at each potential target location.

The temporally extended search task with eye movements introduces two new requirements for the ideal searcher: optimal integration of responses across fixations, and optimal selection of successive fixation locations. The flow diagram of processing performed by the ideal searcher is shown in Fig. 3a. During the first fixation the searcher captures responses from all potential target locations. It then computes the posterior probability that the target is located at each of these locations. If the maximum of the posterior probabilities exceeds a criterion (the criterion determines the error rate), the search stops and the location with the largest posterior probability is reported. If the criterion is not exceeded, the ideal searcher determines the fixation location that will maximize the probability of finding the target after the eye movement is made. It then moves its eyes to that location, and the process repeats.

To integrate responses across fixations optimally, the ideal searcher cumulates the weighted responses from each potential target location:

$$p_i(T) = \frac{\text{prior}(i) \exp\left(\sum_{t=1}^T d'_{ik(t)}{}^2 W_{ik(t)}\right)}{\sum_{j=1}^n \text{prior}(j) \exp\left(\sum_{t=1}^T d'_{jk(t)}{}^2 W_{jk(t)}\right)} \quad (1)$$

where t is fixation number, and $d'_{ik(t)}$ and $W_{ik(t)}$ are the visibility and response at display location i when the fixation is at display location $k(t)$. Equation (1) is for the case in which both stimulus noise and internal noise are statistically independent in time (dynamic). Equations for the more complicated case, in which the noise is a mixture of static stimulus noise and dynamic internal noise (like the present experiments), are given in the Supplementary Information. The predictions reported here are for the static case, although predictions for the dynamic case are similar (see Methods).

To compute the optimal next fixation point, $k_{\text{opt}}(T+1)$, the ideal searcher considers each possible next fixation and picks the location that, given its knowledge of the current posterior probabilities and visibility map, will maximize the probability of correctly identifying the location of the target after the fixation:

$$k_{\text{opt}}(T+1) = \arg \max_{k(T+1)} \left(\sum_{i=1}^n p_i(T) p(C|i, k(T+1)) \right) \quad (2)$$

Maximizing accuracy is the relevant goal in the present task; other goals (such as minimizing entropy) have been explored for certain computer vision tasks¹⁸. Explicit expressions for equation (2) are derived in the Supplementary Information.

Given the prior probabilities of possible target locations and the visibility maps, which specify all the relevant values of d' , equations (1) and (2) can be used to simulate the behaviour of the ideal searcher (see Methods). Figure 3b shows a sequence of ideal fixations. The ideal searcher performs a rather random-looking search pattern, although it is in fact a highly principled search that reflects the specific properties of the stimulus and the visibility map. This figure also shows how posterior probabilities across the display evolve over time. The location of the target is at the peak in the posterior probability map seen downward of the left of centre.

The ideal searcher shows several other interesting qualitative behaviours. First, it sometimes makes fixations to the display location with the maximum posterior probability of containing the target (MAP fixations, where MAP is short for maximum *a posteriori*), and sometimes to a location near the centroid of a cluster of locations where the posterior probabilities are high ('centre-of-gravity' fixations). Both MAP and centre-of-gravity fixations have been observed in human visual search^{19–21}. Second, the saccade lengths of the ideal searcher tend to be moderate in size, because posterior probabilities at nearby locations are pushed down and posterior probabilities at distant locations tend not to jump up (see Fig. 3b). Human saccade lengths also tend to be moderate in

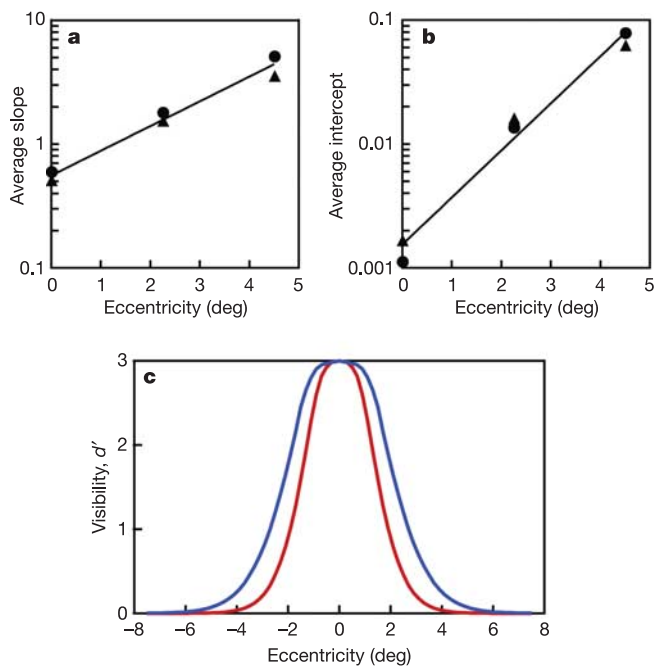


Figure 2 Representation of the visibility maps. **a**, **b**, The average slopes (**a**) and intercepts (**b**) of the threshold functions shown in Fig. 1c, d as a function of retinal eccentricity. Observers: circles, J.N.; triangles, W.G. **c**, The signal-to-noise ratio, d' , for target detection across the visual field (visibility maps) for two of the conditions in the search experiment. The red function is for a background contrast of 0.05 and a target contrast of 0.07. The broader blue function is for a background contrast of 0.20 and a target contrast of 0.19. Note that visibility reaches a peak in the centre of the fovea and decreases rapidly with retinal eccentricity.

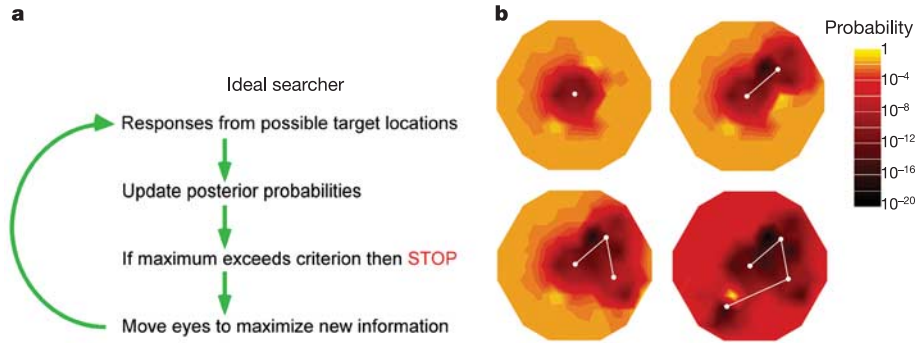


Figure 3 Ideal searcher. **a**, Flow chart for the ideal searcher. **b**, A typical sequence of fixations for the ideal searcher, for which the initial fixation is at the centre of the display. The temperature plots show the posterior probability map after each fixation. There is an

elevated posterior probability at the target location (downward of the left of centre), but initially the eye is drawn to other locations. Posterior probabilities are suppressed in the neighbourhood of each fixation, creating ‘inhibition of return’.

size (see later). Third, the ideal searcher tends not to fixate display locations that it has recently fixated (‘inhibition of return’), again because nearby posterior probabilities are pushed down (see Fig. 3b). Fourth, the ideal searcher sometimes makes long saccades into regions where the posterior probabilities are low, followed by a return saccade to a region with higher probabilities. It performs these eye movements because excluding an unlikely region that has not yet been inspected is sometimes the best chance for increasing the posterior probabilities in the more likely regions. It is unknown whether humans perform these ‘exclusion saccades’ in visual search, although a related type of saccade is predicted for optimal eye movements in reading²².

To compare human and ideal search quantitatively, we measured search performance for the sine-wave target randomly embedded at one of 85 locations tiling the 15° diameter display in a triangular array. Measurements were made for two levels of 1/f noise contrast (0.05 and 0.2) and for six levels of target visibility in the fovea ($d' = 3, 3.5, 4, 5, 6$ and 7). The visibilities were set by using the results from the detection experiment (see Figs 1 and 2). The data points in Fig. 4a show the median number of fixations required for two human observers to find the target. (We obtained a similar search performance for a third observer naive to the aims of the study, although we do not have visibility maps for that observer.) As can be seen, search performance improves as the visibility of the target increases and is better in the high-noise condition (presumably because the visibility maps are broader; see Fig. 2c). The solid curves show the predictions of the ideal searcher with the same visibility maps as the human observers. Figure 4b shows how human and ideal search performance varies with location of the target in the display, for all 12 stimulus conditions. The results in Fig. 4a, b imply that humans are remarkably efficient at visual search, at least under these conditions, nearly reaching the performance of the ideal searcher.

The obvious question is: How do humans perform so well? To address this question, consider the three things that the ideal searcher does in an optimal fashion: parallel detection, integration of information across fixations, and selection of the next fixation location. With regard to parallel detection, there is evidence that humans are efficient at finding targets in noise under conditions in which visibility is equal at all potential target locations^{4,23}. Further, in brief presentations that do not allow eye movements, humans often process multiple target locations in parallel with equal efficiency^{11,23,24}. Our results indicate strongly that humans are able to perform this kind of efficient parallel processing in complex extended search tasks.

With regard to the integration of information across fixations, there is evidence that humans are not very efficient^{8–10}. So how can they approximate ideal performance? A key insight is provided by

the solid curve in Fig. 4c, which plots the average posterior probability at the target location as a function of the number of fixations before the one at which the ideal searcher found the target. The rapid rise in posterior probability implies that there is little to be gained by integrating detailed display or posterior probability information more than one or two fixations into the past. However,

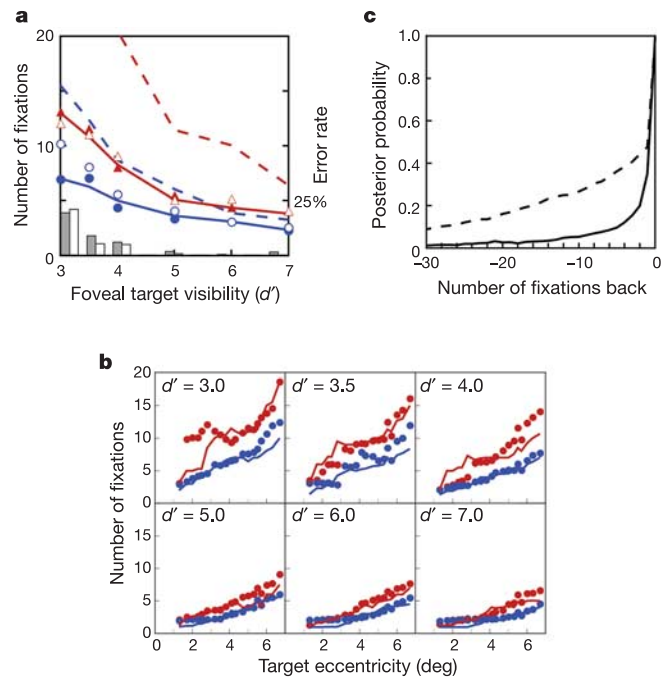


Figure 4 Human versus ideal performance. **a**, Median number of fixations to locate the target correctly, as a function of the target’s visibility in the fovea, for two levels of background noise contrast: 0.05 (red lines and triangles) and 0.20 (blue lines and circles). Solid and dashed curves are the predictions of the ideal and random searchers, respectively. The histogram at the bottom shows the error rates of the human observers (grey) and an ideal searcher (white). Observers: filled symbols, J.N.; open symbols, W.G. **b**, Median number of fixations to locate the target correctly as a function of the target’s eccentricity and its visibility in the fovea. The symbols are combined results for two observers; the solid curves are the predictions of the ideal searcher. The medians were obtained by binning with a sliding 2° window. The medians are less reliable at small eccentricities because the average number of observations in a bin increases with the square of the eccentricity. Noise contrast: red, 0.05; blue, 0.20. **c**, Posterior probability at the target location as a function of the number of fixations before the one in which the searcher found the target. Solid and dashed curves are the predictions of the ideal and random searchers, respectively.

simulations show that to achieve human performance levels it is necessary to have some coarse memory for past fixation locations so as to reduce the likelihood of returning to the same display region.

With regard to the selection of fixation locations, there is little evidence about human efficiency. To examine this issue we simulated searchers that do not select fixation locations optimally but are otherwise ideal. For example, the dashed curves in Fig. 4a show the performance of a searcher that computes posterior probabilities and integrates information across fixations optimally, but makes random fixations. Humans far outperform this random searcher. They also outperform an enhanced version with the added feature of not fixating the same location twice. The fact that humans outperform these searchers rejects all possible models of visual search where fixation locations are selected at random, with or without replacement. We have also evaluated a sub-optimal searcher that always fixates the location with the maximum posterior probability (the MAP searcher). This searcher performs almost as well as the ideal (0.5–2 fixations slower), and thus MAP fixations alone (no centre-of-gravity fixations) are sufficient to approach the efficiency of human fixation selection.

The fixation selection strategies of the searchers can also be compared by examining eye movement statistics. For example, the distributions of saccade length for the humans and the ideal searcher are similar: both are skewed to the right and reach a peak at about 3°, although the ideal distribution is more skewed than the human. The distribution for the random searcher is symmetrical and reaches a peak at about 7°. The distribution for the MAP searcher is similar to the ideal and the human, but less skewed than the human. We also examined the spatial distribution of fixation locations within the display. For both human and ideal searchers the average distribution of fixation locations across the display has a 'doughnut' shape that reaches a peak at about 5° from the centre. Interestingly, the MAP searcher does not have a doughnut-shaped distribution, indicating that humans are not well modelled as MAP searchers.

The present study is another example of how bayesian ideal observer analysis can provide valuable insight into sensory and perceptual processing^{5,6,22}. The ideal searcher is, in some ways, complementary to existing computational models of visual search^{25,26}. Unlike these previous approaches, it is not a heuristic model that can be applied to arbitrary stimuli but a formal, parameter-free analysis for a particular class of naturalistic stimuli. The ideal searcher is not meant to be a plausible model of human visual search (for example, humans do not have perfect memory), but a rigorous starting point for developing models. It remains to be determined what algorithms the brain uses to achieve near-optimal performance for our stimuli, how those algorithms are implemented in neural circuits, and how well those algorithms perform on a more general range of stimuli (for example, on natural images). Nonetheless, it is clear that humans compute something close to an accurate posterior probability map and then use that map to determine the next fixation location efficiently. They are able to reach near-optimal performance, despite relatively poor memory for visual detail and poor integration of information across fixations, because all that is actually needed is a coarse memory sufficient to support the inhibition of return. □

Methods

Stimuli and apparatus

Stimuli were presented on a calibrated monochrome Image Systems monitor (M21L) with a white phosphor (P-104) and resolution 1024 × 768 at 60 Hz. The target was a 6 cycles deg⁻¹ sine-wave grating, tilted 45° to the left and windowed by a symmetrical raised cosine (half-height width one cycle). The background was filled with 1/f noise at a mean luminance of 40 cd m⁻²; the display outside the background was set to the mean luminance. The 1/f noise was created by filtering gaussian white noise, truncating the filtered noise waveform to ±2 s.d., and scaling to obtain the desired r.m.s. amplitude. Eye position was measured with a Forward Technologies SRI Version 6 dual Purkinje eye tracker. Head position was maintained with a bite bar and headrest.

Detection experiment

On each trial, the observer fixated a dot at the centre of the display (there was no fixation dot for foveal measurements). The fixation dot disappeared at the onset of the test stimuli, which consisted of two 250-ms intervals separated by 500 ms. One interval contained background noise alone, the other a different random sample of background noise with the target added. The observer judged which interval contained the target. If the observer's fixation was not within 0.75° of the fixation dot when the test stimuli appeared, the trial was discarded. Within a session the target always appeared in the same location, which was indicated after each trial. Sixteen blocks (four target contrasts × four noise levels) of 32 trials were run in each session. The data for each noise level, in each session, were fitted with a Weibull function:

$$f(c) = 0.5 + 0.5[1 - \exp\{- (c/c_T)^s\}] \quad (3)$$

Both the 82% correct threshold parameter c_T and the steepness parameter s were estimated by using maximum-likelihood methods.

Search experiment

On each trial, the observer first fixated a dot at the centre of the display and then initiated the trial with a button press. The fixation dot disappeared immediately and a random time later (100–500 ms) the search display appeared. The observer's task was to find the target as rapidly as possible and to press a button as soon as the target was located. The observer then indicated the judged target location by fixating that location and pressing the button again. The response was considered correct if the eye position at the time of the second button press was closer to the target location than to any other potential target location. Each session consisted of 6 blocks of 32 search trials. In each session the background noise contrast was fixed. Before each block, the eye tracker was calibrated and the search target for that block was shown on a uniform background at the centre of the display. The set of 12 conditions was repeated 6 times in a counterbalanced fashion.

Search simulations

The solid curves in Figs 1c, 1d, 2a and 2b describe how the threshold parameter $c_T(e_n, \epsilon)$ varied with noise contrast power e_n and eccentricity e . The steepness parameter of the psychometric functions varied with eccentricity from a value of 2 in the fovea to more than 4 in periphery, and was well approximated by $s(e) = 2.8e/(e + 0.8) + 2$. These descriptive models were substituted into equation (3) to obtain a formula for detection accuracy: $f(c, e_n, \epsilon)$. The visibility map was obtained by taking the inverse standard normal integral of the accuracy: $d'(c, e_n, \epsilon) = \sqrt{2} \Phi^{-1}(f(c, e_n, \epsilon))$. The factor 2 takes into account that there were two intervals in the forced choice detection task, but (effectively) only one interval in each fixation of the search task³. The visibility maps were obtained by averaging across all directions; in fact, the visibility maps are not radially symmetric but fall off rather faster in the vertical direction than in the horizontal direction. Using the radial average has no effect on the predictions described here.

Here we describe the simulations for the case in which the external and internal noise is statistically independent (dynamic) in time; the Supplementary Information describes the case in which the external noise is static. We note first that the template responses at each location can be given an expected value of 0.5 when the target is at that location, and -0.5 otherwise. This has no effect on the predictions as long as we add enough noise to the simulated template responses to make the values of d' exactly those given by the visibility map. The six steps for each simulated search trial were as follows. First, fixation began at the centre of the display (as in the search experiment). Second, a target location was selected at random (prior(i) = 1/85); 0.5 was added to that location and -0.5 to all other locations. Third, a gaussian noise sample was generated for each of the 85 potential target locations. The standard deviation of each noise sample was set to be consistent with the value of the visibility map at that location: $\sigma = 1/d'$. Fourth, the posterior probability for each potential target location was calculated from equation (1). Fifth, if the maximum posterior probability exceeded a criterion, the search stopped. The criterion for each condition was picked so that the error rate of the ideal searcher approximated that of the humans. Sixth, for the ideal searcher, equation (2) was evaluated to select the next fixation location; for the random searcher, the next fixation location was selected at random. The process then jumped back to the third step. Note that the specific characteristics of the target and 1/f noise enter the simulation through the visibility maps. Also note that although 1/f noise is spatially correlated, we verified by simulation that the template responses were effectively uncorrelated. The ideal searcher performs slightly better in the dynamic case than in the static case, because it gains more information on each fixation, but the predicted curves are nearly parallel.

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The first cleavage of the mouse zygote predicts the blastocyst axis

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One of the unanswered questions in mammalian development is how the embryonic–abembryonic axis of the blastocyst is first established. It is possible that the first cleavage division contributes to this process, because in most mouse embryos the progeny of one two-cell blastomere primarily populate the embryonic part of the blastocyst and the progeny of its sister populate the abembryonic part^{1–4}. However, it is not known whether the embryonic–abembryonic axis is set up by the first cleavage itself, by polarity in the oocyte that then sets the first cleavage plane with respect to the animal pole, or indeed whether it can be divorced entirely from the first cleavage and established

in relation to the animal pole. Here we test the importance of the orientation of the first cleavage by imposing an elongated shape on the zygote so that the division no longer passes close to the animal pole, marked by the second polar body. Non-invasive lineage tracing shows that even when the first cleavage occurs along the short axis imposed by this experimental treatment, the progeny of the resulting two-cell blastomeres tend to populate the respective embryonic and abembryonic parts of the blastocyst. Thus, the first cleavage contributes to breaking the symmetry of the embryo, generating blastomeres with different developmental characteristics.

It has been shown, either by marking cells directly or by relating their position to external markers, that the majority of first cleavage divisions generate one blastomere whose progeny will primarily populate the embryonic part of the blastocyst (polar trophectoderm and deeper cells of the inner cell mass) and another whose progeny populate the abembryonic part (mural trophectoderm and the more superficial inner cell mass)^{1–4}. More recently, further lineage tracing experiments have clarified this relationship and shown that, by the four-cell stage of normally developing embryos, blastomeres not only have specific fates but can also differ in their developmental potential^{5,6}. Static observations and a series of micromanipulation experiments to relocate the animal pole of the mouse zygote indicate that in normal circumstances the first cleavage usually passes close to this pole^{7,8}. A second marker of the first cleavage, the sperm entry site¹, reflects positioning of the spindle in relation to a slight flattening of the zygote at fertilization⁹. Together these observations raise the question of whether it is the spatial organization of the zygote with respect to the animal pole or, because cleavage orientation can reflect the random site of sperm entry, cleavage itself that influences the subsequent development of the embryonic–abembryonic axis.

To approach this question, we first developed a better method for accurate three-dimensional examination of the first cleavage orientation in a random population of zygotes. We achieved this by time-lapse observations of the first cleavage on multiple focal planes at each time point. In addition, to facilitate analysis of the position of the first cleavage plane in respect to pronuclei (and the polar body (PB)), we followed this cleavage in a newly developed transgenic line (CAG:H2B–EGFP) in which chromatin was labelled green by the expression of green fluorescent protein (GFP)-tagged histone H2B (ref. 10; Fig. 1a; Supplementary Movie 1). We found that the female pronucleus was closer to the PB than the male pronucleus in 87.5% ($n = 32$) of zygotes (categories I–III; Fig. 1b) and that in most zygotes (category I, 62.5%) the two pronuclei were aligned with the PB and the cleavage furrow formed within 30° of this plane. In 12.5% of zygotes (category II), the pronuclei were displaced from the PB by between 30° and 90° and the cleavage plane was displaced to a similar extent. In the two remaining categories, cleavage passed within 30–90° of PBs aligned with the pronuclei (category III), and within 30° of PBs not aligned with the pronuclei (category IV). We observed that this most frequent alignment of the differentially condensed¹¹ female and male pronuclei with the PB was maintained into prometaphase. Immunostaining of fixed zygotes to reveal CpG-methylated female chromatin showed that, in agreement with previous studies^{11,12} and contrary to a recent proposition¹³, the parental sets of chromosomes did not undergo mixing and adopted an arrangement consistent with our time-lapse studies that was retained into the daughter blastomeres (Fig. 1c).

To characterize the orientation of the cleavage plane further, we performed time-lapse differential interference contrast (DIC) microscopy on zygotes of a different, wild-type mouse strain (Fig. 1d). By observing multiple focal planes we ensured that we could follow cleavage in relation to the location of markers in three dimensions in 96% of all randomly positioned zygotes. We found that the onset of cleavage furrow formation was within 30° of the PB in 70% of zygotes, 14-fold greater than at a lateral position between

Optimal Eye Movement Strategies in Visual Search (Supplement)

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Here we derive the ideal searcher for the case of dynamic (temporally uncorrelated) external and internal noise, and we describe (without proof) the ideal searcher for the case of static (temporally correlated) external noise and dynamic (temporally uncorrelated) internal noise. As a check on the accuracy of the formulas for these ideal searchers, they were derived via two separate methods: a direct derivation from the joint probability distributions (WG) and a derivation based upon the theory of Kalman filtering (JN).

The visibility map

To derive the ideal searcher it is necessary to consider the meaning of the visibility map in more detail. To do this we describe the ideal detector for a known sine wave target presented at a known location in a single interval forced choice task.

First, consider an ideal detector with direct access to the retinal image; that is, an ideal detector for a non-foveated visual system. Each trial of a single interval forced choice task consists either of background noise alone or background noise plus the sine wave target. The ideal detector multiplies the retinal image with a template of the sine wave target and then integrates the product to obtain a template response W (i.e., the template response is the cross correlation of the target with the retinal stimulus). The magnitude of this template response is then compared to a criterion; the optimal behavior is to respond “yes” if the template response exceeds the criterion and “no” otherwise. The accuracy of this ideal detector is determined by the signal-to-noise ratio, d' , which is the average difference in the template response to the background plus target and background, divided by the standard deviation of the template response^{1,2}. The expected value of the template response to background plus target is proportional to the target contrast and the variance of the template response is proportional to the noise contrast power of the background, and hence

$$d'(c, e_n)^2 = \frac{Ac^2}{Be_n} \tag{S1}$$

where, c is the RMS contrast of the target, e_n is the contrast power of the noise background, and A and B are proportionality constants.

Now consider an ideal detector in a foveated visual system. In this case, the ideal detector does not have direct access to the retinal image, but instead to a representation that is degraded by variable spatial resolution and neural noise. Reduced spatial resolution due to spatial filtering will effectively reduce the contrast of a sine wave target, but will have little effect on the shape of the target, thus the same template can be used in regions of reduced resolution, although the responses to the target and background will be smaller. (We have verified that for our target and

for eccentricities as large as the radius of our display, the appropriate template shape changes negligibly for transfer functions that match human contrast sensitivity functions.) Furthermore, the neural noise will add a term $C(c, e_n, \varepsilon)$ to the variance of the template responses. In general, this neural noise term may depend on the target contrast, the background noise power, and the eccentricity. Therefore, the visibility map of an ideal detector with a foveated visual system is given by

$$d'(c, e_n, \varepsilon)^2 = \frac{A(\varepsilon)c^2}{B(\varepsilon)e_n + C(c, e_n, \varepsilon)} \quad (\text{S2})$$

where the proportionality factors on the template responses to the target and background now vary with eccentricity. Without loss of generality this formula can be simplified by dividing numerator and denominator by $A(\varepsilon)$:

$$d'(c, e_n, \varepsilon)^2 = \frac{c^2}{\alpha e_n + \beta(c, e_n, \varepsilon)} \quad (\text{S3})$$

where $\alpha = B(\varepsilon)/A(\varepsilon)$ and $\beta(c, e_n, \varepsilon) = C(c, e_n, \varepsilon)/A(\varepsilon)$. Because the same shaped template is used at different eccentricities, the value of α is a constant that does not change with eccentricity. Equation (S3) gives the visibility map of the ideal detector, once the values of α and β are specified for all eccentricities. We note, however, that in the case of dynamic (temporally uncorrelated) external and internal noise, the two noise sources are of the same type and so their combined effect is given directly by the psychophysically measured visibility map $d'(c, e_n, \varepsilon)$. In the case of static external noise and dynamic internal noise, the two noises have different effects and so it is necessary to specify α and $\beta(c, e_n, \varepsilon)$ separately (see later).

Ideal searcher for dynamic external and internal noise

Let n be the number of potential target locations, and let $W_{ik(t)}$ be the Gaussian-distributed template response from the i^{th} potential target location, at fixation t , with fixation location $k(t)$. Without loss of generality, we can set the expected value of $W_{ik(t)}$ to 0.5, when the target is present at that location, and to -0.5, otherwise. This has no affect on the predictions as long as we set the standard deviation of the template responses so as to preserve the value of d' specified by the visibility map. Thus, the mean value of the template response is

$$u_{ik(t)} = \begin{cases} 0.5 & i = \text{target location} \\ -0.5 & i \neq \text{target location} \end{cases} \quad (\text{S4})$$

and the variance of the template response is

$$\sigma_{ik(t)}^2 = \frac{1}{d'_{ik(t)}{}^2} \quad (\text{S5})$$

Updating posterior probabilities. We now derive the following formula, which gives the posterior probability that the target is at location i after T fixations:

$$p_i(T) = \frac{\text{prior}(i) \exp \left[\sum_{t=1}^T d'_{ik(t)}{}^2 W_{ik(t)} \right]}{\sum_{j=1}^n \text{prior}(j) \exp \left[\sum_{t=1}^T d'_{jk(t)}{}^2 W_{jk(t)} \right]} \quad (\text{S6})$$

This formula (which is equation (1) in the main body of the report) shows that to perfectly integrate information across fixations it is sufficient to keep a running weighted sum of the template responses at each potential target location, where the weights are the squares of the visibility map values.

Note first that all the template responses collected at fixation t can be represented by a vector, $\mathbf{W}(t) = (W_{1k(t)}, \dots, W_{nk(t)})$. Using Bayes' formula, it follows immediately that the posterior probability that the target is at location i after T fixations is given by

$$p_i(T) = \frac{\text{prior}(i) p(\mathbf{W}(1), \dots, \mathbf{W}(T) | i)}{\sum_{j=1}^n \text{prior}(j) p(\mathbf{W}(1), \dots, \mathbf{W}(T) | j)} \quad (\text{S7})$$

Both the external noise and internal noise are statistically independent over time, and for potential target locations separated sufficiently in space (as in the present search experiments) the external noise and internal noise are also statistically independent over space. Thus,

$$p_i(T) = \frac{\text{prior}(i) \prod_{t=1}^T \prod_{q=1}^n p(W_{qk(t)} | i)}{\sum_{j=1}^n \text{prior}(j) \prod_{t=1}^T \prod_{q=1}^n p(W_{qk(t)} | j)}$$

Given equations (S4) and (S5), and the fact that the template responses are Gaussian distributed, we have

$$p_i(T) = \frac{\text{prior}(i) \frac{(2\pi)^{-T/2}}{\prod_{t=1}^T \sigma_{ik(t)}} \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{ik(t)} - 0.5)^2}{\sigma_{ik(t)}^2}\right) \prod_{q \neq i} \left(\frac{(2\pi)^{-T/2}}{\prod_{t=1}^T \sigma_{qk(t)}} \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{qk(t)} + 0.5)^2}{\sigma_{qk(t)}^2}\right) \right)}{\sum_{j=1}^n \text{prior}(j) \frac{(2\pi)^{-T/2}}{\prod_{t=1}^T \sigma_{jk(t)}} \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{jk(t)} - 0.5)^2}{\sigma_{jk(t)}^2}\right) \prod_{q \neq j} \left(\frac{(2\pi)^{-T/2}}{\prod_{t=1}^T \sigma_{qk(t)}} \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{qk(t)} + 0.5)^2}{\sigma_{qk(t)}^2}\right) \right)}$$

Dividing the numerator and denominator by the numerator gives,

$$p_i(T) = \frac{1}{1 + \sum_{j \neq i} \frac{\text{prior}(j)}{\text{prior}(i)} \frac{\exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{jk(t)} - 0.5)^2}{\sigma_{jk(t)}^2}\right) \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{ik(t)} + 0.5)^2}{\sigma_{ik(t)}^2}\right)}{\exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{ik(t)} - 0.5)^2}{\sigma_{ik(t)}^2}\right) \exp\left(-\sum_{t=1}^T \frac{1}{2} \frac{(W_{jk(t)} + 0.5)^2}{\sigma_{jk(t)}^2}\right)}$$

After combining terms we have,

$$p_i(T) = \frac{1}{1 + \sum_{j \neq i} \frac{\text{prior}(j)}{\text{prior}(i)} \exp\left(\sum_{t=1}^T \frac{W_{jk(t)}}{\sigma_{jk(t)}^2} - \sum_{t=1}^T \frac{W_{ik(t)}}{\sigma_{ik(t)}^2}\right)}$$

Finally, equation (S6) is obtained by using equation (S5) to substitute for the variances, and then by multiplying the numerator and denominator by $\text{prior}(i) \exp\left[\sum_{t=1}^T d'_{ik(t)} {}^2 W_{ik(t)}\right]$.

Selecting next fixation location. To compute the optimal next fixation point, $k_{opt}(T+1)$, the ideal searcher considers each possible next fixation and picks the location that, given its knowledge of the current posterior probabilities and the visibility map, will maximize the probability of correctly identifying the location of the target after the next fixation is made:

$$k_{opt}(T+1) = \arg \max_{k(T+1)} \left(p(C|k(T+1)) \right)$$

Conditioning on the target location gives the following equation, which is equation (2) in the main body of the report:

$$k_{opt}(T+1) = \arg \max_{k(T+1)} \left(\sum_{i=1}^n p_i(T) p(C|i, k(T+1)) \right) \quad (\text{S8})$$

Here we derive a version of this equation that is practical to evaluate in computer simulations.

The probability of each possible target location is given by equation (S6), thus our job is to derive an expression for $p(C|i, k(T+1))$, the probability of being correct given that the true target location is i , and the location of the next fixation is $k(T+1)$. Let Z_j be the hypothetical template response from the j^{th} location after the next fixation is made; i.e., $Z_j = W_{jk(T+1)}$. After making the next fixation, the decision rule that would maximize accuracy would be to pick the location with the maximum posterior probability. If one uses that decision rule, then the percent correct is equal to the probability that the posterior probability at location i will be greater than that at all other locations:

$$p(C|i, k(T+1)) = p(p_i(T+1) \geq p_1(T+1), \dots, p_i(T+1) \geq p_n(T+1) | i, k(T+1))$$

or equivalently,

$$p(C|i, k(T+1)) = p(L_{i1} \geq 1, \dots, L_{in} \geq 1 | i, k(T+1)) \quad (\text{S9})$$

where L_{ij} is the ratio of the posterior probabilities for location i and location j . From equation (S6) we have

$$L_{ij} = \frac{\text{prior}(i) \exp \left[\sum_{t=1}^{T+1} d'_{ik(t)} {}^2 W_{ik(t)} \right]}{\text{prior}(j) \exp \left[\sum_{t=1}^{T+1} d'_{jk(t)} {}^2 W_{jk(t)} \right]}$$

which can be partitioned into the currently known posterior probabilities $p_i(T)$ and $p_j(T)$, and the currently unknown template responses that will occur after the next fixation. Thus,

$$L_{ij} = \frac{\exp\left[d'_{ik(T+1)}{}^2 Z_i\right] p_i(T)}{\exp\left[d'_{jk(T+1)}{}^2 Z_j\right] p_j(T)}$$

Note that the L_{ij} are statistical dependent, but become statistically independent if we condition on the value of Z_i . Thus,

$$p(C|i, k(T+1)) = \int_{-\infty}^{\infty} p(z_i) \prod_{i \neq j} p\left(\frac{\exp\left[d'_{ik(T+1)}{}^2 z_i\right] p_i(T)}{\exp\left[d'_{jk(T+1)}{}^2 Z_j\right] p_j(T)} \geq 1\right) dz_i$$

or,

$$p(C|i, k(T+1)) = \int_{-\infty}^{\infty} p(z_i) \prod_{i \neq j} p\left(Z_j < \frac{\ln\left(\frac{p_j(T)}{p_i(T)}\right) + d'_{ik(T+1)}{}^2 z_i}{d'_{jk(T+1)}{}^2}\right) dz_i$$

Expressing this equation in terms of the standard normal distribution we have

$$p(C|i, k(T+1)) = \int_{-\infty}^{\infty} d'_{ik(T+1)} \phi\left(d'_{ik(T+1)}(z_i - 0.5)\right) \prod_{i \neq j} \Phi\left(\frac{\ln\left(\frac{p_j(T)}{p_i(T)}\right) \frac{1}{d'_{jk(T+1)}{}^2} + \frac{d'_{ik(T+1)}{}^2}{d'_{jk(T+1)}{}^2} z_i + 0.5}{\frac{1}{d'_{jk(T+1)}{}^2}}\right) dz_i$$

where $\phi(x)$ is the standard normal density function and $\Phi(x)$ is the standard normal integral function: $\phi(x) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}x^2\right)$, $\Phi(x) = \int_{-\infty}^x \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}y^2\right) dy$. Finally, making the change of variable $w = d'_{ik(T+1)}(z_i - 0.5)$, we have

$$p(C|i, k(T+1)) = \int_{-\infty}^{\infty} \phi(w) \prod_{j \neq i} \Phi \left(\frac{-2 \ln \frac{p_j(T)}{p_i(T)} + d'_{jk(T+1)}{}^2 + 2d'_{ik(T+1)}w + d'_{ik(T+1)}{}^2}{2d'_{jk(T+1)}} \right) dw \quad (\text{S10})$$

Although this formula contains an integral it can be evaluated rapidly using numerical integration, because the standard normal density function approaches zero rapidly away from the origin. This formula reduces to the well-known formula for accuracy in the n-alternative forced choice task², in the special case that all the priors are equal and all the values of d' are equal. In sum, equations (S6), (S8) and (S10), and the measured visibility map (equation S3) can be used to simulate optimal visual search in the dynamic noise case.

Ideal searcher for static external noise and dynamic internal noise

The ideal searcher for static external noise is basically the same as for dynamic external noise, except that we must consider the external and internal noise separately. Note first that equation (S3) partitions the noise that limits detection performance into two parts, the static part due to the external noise (αe_n) and the dynamic part due to the internal noise ($\beta(c, e_n, \varepsilon)$). We directly determined the value of α (0.0218) by measuring the template responses to the target and by measuring the variance of the template responses to very large number of samples of the actual background noise used in the experiments. Given the value of α , the variance of the dynamic internal noise can be determined from the measured visibility maps (the values of $d'(c, e_n, \varepsilon)$), using equation (S3).

To simulate the ideal searcher's performance, we generated a static noise sample of standard deviation $\sqrt{\alpha e_n}/c$ for each potential target location, before the first fixation. Then, on each fixation, for each potential target location, we generated a dynamic noise sample of standard deviation $\sqrt{\beta(c, e_n, \varepsilon)}/c$, which we added to the static noise sample at that location. Otherwise, the simulation was run in the same fashion as for dynamic case (see the methods section in the report). We now state (without proof) the formulas for the ideal searcher when the external noise is static.

Updating posterior probabilities. The optimal integration of the template responses across fixations is given by the following three equations:

$$p_i(T) = \frac{\text{prior}(i) \exp \left[\sum_{t=1}^T g_{ik(t)}(T) W_{ik(t)} \right]}{\sum_{j=1}^n \text{prior}(j) \exp \left[\sum_{t=1}^T g_{jk(t)}(T) W_{jk(t)} \right]} \quad (\text{S11})$$

$$\mathbf{g}_{ik(t)}(T) = \frac{c^2}{e_n \alpha \beta_{ik(t)} v_i(T) + \beta_{ik(t)}} \quad (\text{S12})$$

$$v_i(T) = \sum_{r=1}^T \frac{1}{\beta_{ik(r)}} \quad (\text{S13})$$

These equations reflect the fact that the ideal searcher averages out the internal noise over time (because it is dynamic), and hence obtains an ever-improving estimate of the static noise and static noise plus target.

Selecting next fixation location. Equation (S8) still applies in the static noise case. However, the formulas for $p(C|i, k(T+1))$ are more complicated.

$$p(C|i, k(T+1)) = \int_{-\infty}^{\infty} \phi(w) \prod_{j \neq i} \Phi \left(\frac{\mathbf{g}_{ik(T+1)}(T+1) (\sigma_{ik(T+1)} w + \mu_{ik(T+1)}) + h_{ij}(T+1)}{\mathbf{g}_{jk(T+1)}(T+1) \sigma_{jk(T+1)}} - \frac{\mu_{jk(T+1)}}{\sigma_{jk(T+1)}} \right) dw \quad (\text{S14})$$

$$\mu_{ik(T+1)} = 1 + \frac{c e_n \alpha \sum_{t=1}^T \frac{W_{ik(t)} - 0.5}{\beta_{ik(t)}}}{1 + e_n \alpha v_i(T+1)} \quad (\text{S15})$$

$$\mu_{jk(T+1)} = \frac{c e_n \alpha \sum_{t=1}^T \frac{W_{jk(t)} + 0.5}{\beta_{jk(t)}}}{1 + e_n \alpha v_j(T+1)}, \quad j \neq i \quad (\text{S16})$$

$$\sigma_{jk(T+1)} = \sqrt{\beta_{jk(T+1)} \frac{1 + e_n \alpha v_j(T+1)}{1 + e_n \alpha v_j(T)}}, \quad \forall j \quad (\text{S17})$$

$$h_{ij}(T+1) = \ln \left(\frac{\text{prior}(i)}{\text{prior}(j)} \right) + \sum_{t=1}^T (\mathbf{g}_{ik(t)}(T+1) W_{ik(t)} - \mathbf{g}_{jk(t)}(T+1) W_{jk(t)}) \quad (\text{S18})$$

In sum, equations (S11) - (S18), and the measured visibility map (equation S3) can be used to simulate optimal visual search in the static noise case. Although these formulas are more complicated than for the dynamic noise case, they compute at almost the same speed.

Looking into the future. The sub-optimal searcher that always fixates the location with maximum posterior probability (the MAP searcher) does not consider potential information that will be gained after making eye movements, and hence does not look into the future. The ideal searcher described here considers the probability of localizing the target after the next eye movement, and hence it looks one fixation into the future. Because the ideal searcher looks only one fixation into the future it is a so-called ‘greedy’ algorithm. We have derived formulas for ideal searchers that look more fixations into the future. These algorithms are not practical because of the combinatorial explosion of fixation locations to consider; however, we have compared (for a single search condition) the present ideal searcher with one that is able to look two fixations into the future. This searcher performs slightly better (approximately a quarter of a fixation faster) than the searcher that looks ahead one fixation, which in turn performs better (approximately one fixation faster) than the MAP searcher that looks ahead no fixations. These results demonstrate rapidly diminishing returns for looking further into the future, and thus the present ideal searcher appears to be very close to the true global optimum.

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